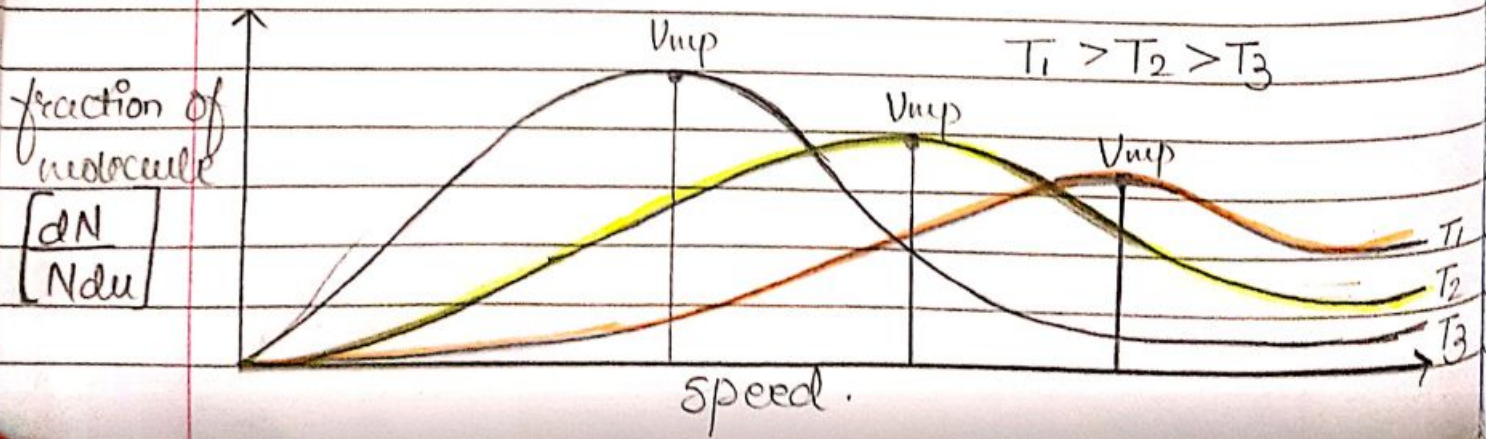
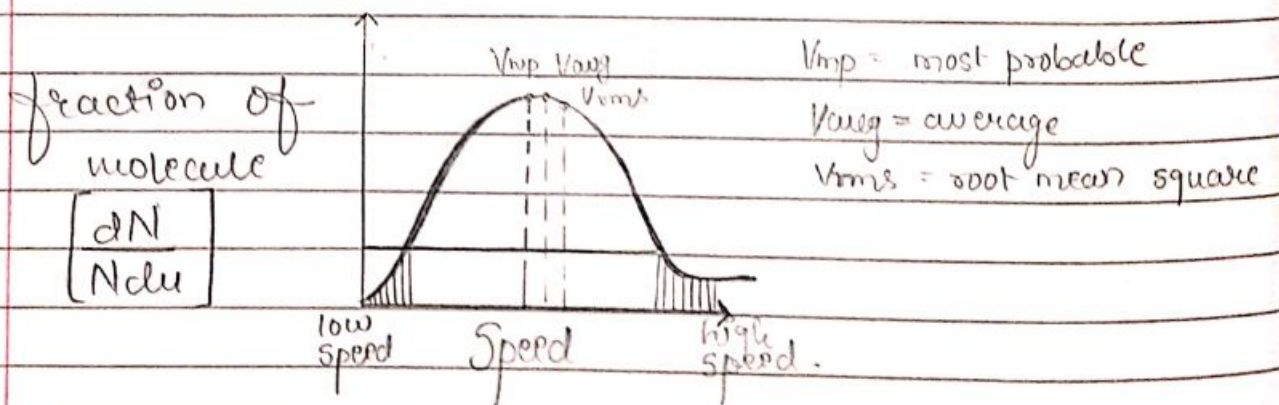


# # Maxwell distribution graph for speed / velocity of gaseous molecule:

- in gas sample at constant temperature all gaseous molecules do not have same speed but they possess a wide range of molecular speed.
- according to Maxwell, in a gas sample at a certain temperature, the number of particles having a particular speed remain constant and can be calculated by Maxwell Differentiation Equation.

eqn

- on the basis of these equation he plotted a graph between
  - fraction of molecules ( $\frac{dN}{Ndu}$ ) & speed of molecule.



\* temperature बढ़ते पर Graph flatten होता है।

## # Conclusion:

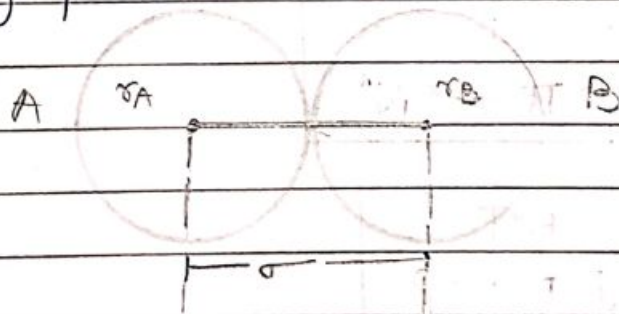
:(5) परमाणु गति (3)

- small fraction of molecule have very low and very high velocities (speed).
- curve flattens on increasing temperature.
- most of the molecules (have most probable) velocity.

## # Collision Parameter: (JEE only)

### (A) collision diameter ( $\sigma$ ):

- closest distance between centre of 2 molecules taking part in collision



### (B) Number density ( $N^*$ ):

- number of molecules per unit volume of gas.

$$N^* = \frac{N}{V}$$

$$(n = \frac{N}{N_A})$$

$$PV = nRT$$

$$PV = \frac{N}{N_A} RT$$

$$\frac{N}{V} = \frac{P N_A}{RT}$$

$\rightarrow kT$   
(Boltzmann's constant)

$$N^* = \frac{N}{V} = \frac{P}{KT}$$

(C) Collision frequency (z):

- number of collision per molecule in per unit time
- mathematically it can be calculated as,

$$z = \sqrt{2} \pi \sigma^2 V_{avg} N^*$$

(D) Mean free path ( $\lambda$ ):

- average distance travelled by a molecule between 2 successive collision:

(Note) - it can be calculated as:

$$\lambda = \frac{V_{avg}}{z}$$

$$\lambda = \frac{1}{\sqrt{2} \pi \sigma^2 N^*}$$

$$\lambda = \frac{KT}{\sqrt{2} \pi \sigma^2 P}$$

Q:27 find ratio of root mean path of molecules of 2 gases having molecular diameter  $1\text{\AA}$  and  $2\text{\AA}$  respectively at constant temperature and pressure.

$$\rightarrow \lambda = \frac{1}{\sqrt{2} \pi \sigma^2 N^*} \quad \therefore \frac{\lambda_1}{\lambda_2} = \left( \frac{\sigma_2}{\sigma_1} \right)^2$$

$$\boxed{4:1}$$

Q:28 if mean free path is (1) at 1 atm then find value at 5 atm. (at constant temperature)

$$\Rightarrow \lambda \propto \frac{T}{P} \quad \therefore \lambda \propto \frac{1}{P}$$

$$\frac{\lambda_1}{\lambda_2} = \frac{P_2}{P_1} \quad \rightarrow \quad \frac{1}{x} = \frac{5}{1} \quad \therefore \boxed{x = \frac{1}{5}}$$

## # Real gas:

- those gases which doesn't follow gaseous law at entire range of pressure, and volume
- all gases are Real Gases; neither of the gas is ideal in nature due to two faulty assumptions of RTG:
  - a) volume of gaseous molecule is negligible as compared to total gas volume.

b) no force of attraction between gaseous molecules.

## #> Compressibility factor (z):

- it is a scale to measure deviation of real gas from their ideal behaviour.

$$\boxed{z = \frac{PV}{nRT}}$$

$$Z = \frac{PV}{RT} \quad (\text{for 1 mole gas})$$

$$Z = \frac{V_{obs}}{V_{ideal}}$$

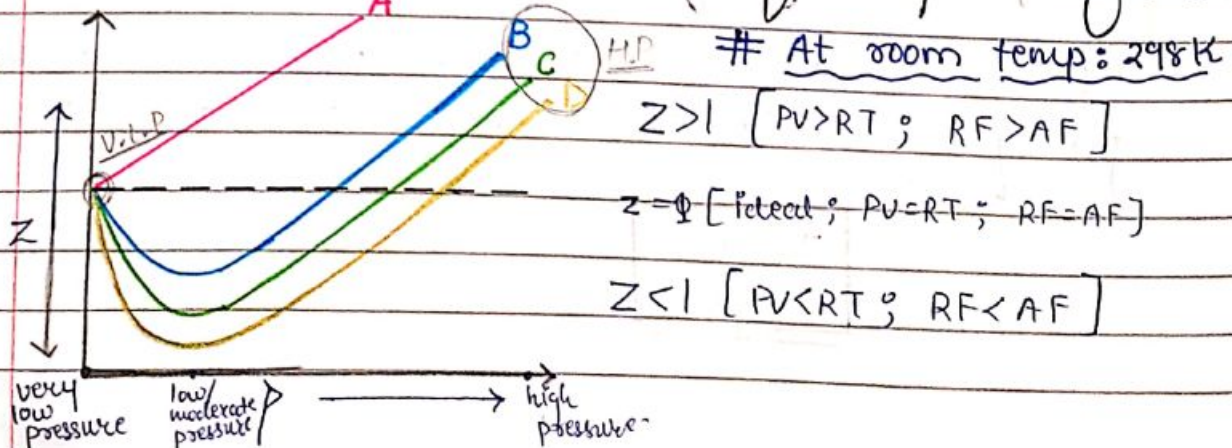
or

$$Z = \frac{V_{real}}{V_{ideal}}$$

	Z ≠ 1 (real gas)		
	Z = 1 (ideal gas)	Z > 1 (+ve deviation)	Z < 1 (-ve deviation)
1.	PV = RT	PV > RT	PV < RT
2.	V <sub>real</sub> = V <sub>ideal</sub>	V <sub>real</sub> > V <sub>ideal</sub>	V <sub>real</sub> < V <sub>ideal</sub>
3.	Repulsive f = Attraction f. (Ideal Gas.)	R.F > A.F (Permanent Gas.)	R.F < A.F. (Liquifiable Gas.)
eg:	N <sub>2</sub> ; O <sub>2</sub> .	H & inert gas	HCl; CO <sub>2</sub> ; NH <sub>3</sub> ; SO <sub>2</sub> ; SO <sub>3</sub> ; etc.

\* N<sub>2</sub> and O<sub>2</sub> (nearly ideal behaviour)

### ⇒ Graphical representation of compress factor



- In this graph; - Gas A shows +ve deviation (always).
  - (It is a permanent gas).
  - (It is approximately impossible to convert to liquid state).

- Gas D shows maximum negative (-ve) deviation, and it is more liquified gas as compared to gas B and C.

★ - At low pressure and high temperature real gas behaves as nearly ideal. (due to  $f_{0.01}$  of all  $\downarrow$ )

Q.29 Arrange following gases in increasing order of:
 

- deviation from ideal behaviour.
- liquification.

Gas	A	B	C	D	E
Z	0.8	0.3	1.3	1.2	1.5
deviation of	-0.2	-0.7	+0.3	+0.2	+0.5

⇒

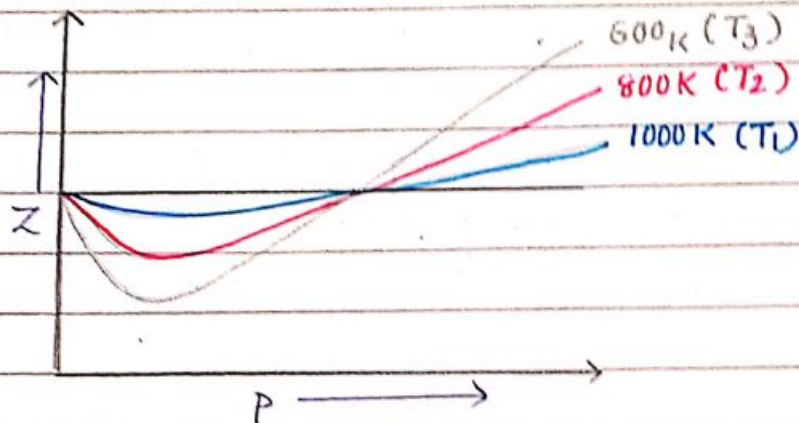
Gas	A	B	C	D	E
Z	0.8	0.3	1.3	1.2	1.5
deviation	-0.2	-0.7	+0.3	+0.2	+0.5

∴ (A) max deviation;  $B > E > C > A \approx D$ .

(B) liquification;  $B > A > D > C > E$ .

- ve  $\uparrow$  to liquification easy.
- +ve  $\uparrow$  to liquification difficult.

## # At high temperatures: [z vs P]



- at very high temperatures, real gas acts nearly same to ideal behaviour due to lessening or decreasing of force of attraction. at high temperature to negligible.

## # Pressure and Volume Correction:

- (A) - due to force of attraction available in real gas molecules so, pressure correction is required in ideal gas condition equation.

$$P_{\text{gas}} = P_{\text{ideal}} - \frac{an^2}{V^2}$$

$$P_i = P_{\text{gas}} + \frac{an^2}{V^2}$$

-  $\frac{an^2}{V}$  = pressure due to force of attraction

- a = vanderwall constant w.r.t. liquification.

[value of 'a' different for variable gases]

(B) - Volume Correction - Actual volume of a gas =  
Vol. of container - Vol. of gaseous particles.

∴ Actual Vol = V - nb

~~Ex. Next~~

here, nb = exclude volume or covolume or abundance volume.  
b = vanderwall constant. w.r.t size of molecule.

\* calculation for value of 'b':

$$b = \frac{4}{3} \times 4 \pi r^3 \times N_A$$
  
voids - vol. of sphere (shape of gas molecule)  $\times$  mole

# Real gas equation: (van-der-waals gas equation). (1)

- after correction of the pressure and volume, vanderwall modified the ideal gas equation and give real gas equation.

$$\left( P + \frac{an^2}{V} \right) (V - nb) = nRT$$

for 1 mole gas:

$$\left( P + \frac{a}{V} \right) (V - b) = RT$$

→ unit of 'a':

$$\text{Pressure} = \frac{an^2}{V}$$

∴,  $a = \frac{\text{atm lit}^2}{\text{mole}^2}$

∴, in MKS =  $\frac{\text{Pa (m}^3\text{)}^2}{\text{mole}^2}$

∴,  $a = \frac{\text{Pa m}^6}{\text{mole}^2}$  (MKS)

→ unit of 'b':

$$\text{Volume} = nb$$

∴,  $b = \frac{\text{lit}}{\text{mole}}$

∴,  $b = \frac{\text{m}^3}{\text{mole}}$

# Value of 'z' at different pressure:

(a) z at very low pressure:

p = very low ↓↓↓  
v = very high ↑↑↑

- In that case;

$a=0$   $b=0$ .

$$\left[ \frac{P+a}{V^2} \right] (V-nb) = RT \quad (n=1 \text{ mole})$$

∴,  $PV = RT$  ( $z=1$ ; gas show ideal behaviour in this case)

(b) z at low pressure:

p = moderate ↓ v = moderate ↑

- In that case;

b = negligible.

$$\left[ \frac{PV^2+a}{V^2} \right] (V-nb) = RT$$