

$$\textcircled{1} 1 \cdot \cos \theta \cdot \sin(90^\circ - \theta) + \sin \theta \cos(90^\circ - \theta) = 1$$

$$\Rightarrow \cos \theta \cdot \cos \theta + \sin \theta \cdot \sin \theta = 1$$

$$\Rightarrow \cos^2 \theta + \sin^2 \theta = 1$$

$$\Rightarrow 1 = 1 \quad \text{proved!!}$$

$$\textcircled{2} \frac{\tan \theta}{\tan(90^\circ - \theta)} + \frac{\sin(90^\circ - \theta)}{\cos \theta} = \sec^2 \theta$$

$$\Rightarrow \frac{\tan \theta}{\cot \theta} + \frac{\cancel{\cos \theta}}{\cancel{\cos \theta}} = \sec^2 \theta$$

$$\Rightarrow \frac{\cancel{\sec^2 \theta} \tan \theta}{1/\tan \theta} + 1 = \sec^2 \theta$$

$$\Rightarrow \tan^2 \theta + 1 = \sec^2 \theta$$

$$\Rightarrow \sec^2 \theta = \sec^2 \theta \quad \text{proved}$$

$$\textcircled{3} \frac{\cos(90^\circ - \theta) \cos \theta}{\tan \theta} + \cos^2(90^\circ - \theta) = 1$$

$$\Rightarrow \frac{\sin \theta \cos \theta}{\tan \theta} + \sin^2 \theta = 1$$

$$\Rightarrow \frac{\sin \theta \cos \theta}{\frac{\sin \theta}{\cos \theta}} + \sin^2 \theta = 1$$

$$\Rightarrow \frac{\sin \theta \cos \theta \cos \theta}{\sin \theta} + \sin^2 \theta = 1$$

$$\Rightarrow \cos^2 \theta + \sin^2 \theta = 1$$

$$\Rightarrow 1 = 1 \quad \text{proved}$$

$$\textcircled{4} \sin(90^\circ - \theta) \cos(90^\circ - \theta) = \frac{\tan \theta}{1 + \tan^2 \theta}$$

$$\Rightarrow \cos \theta \times \sin \theta = \frac{\sin \theta / \cos \theta}{1 + (\sin \theta / \cos \theta)^2}$$

$$\Rightarrow \cos \theta \times \sin \theta = \frac{\sin \theta \times \cos^2 \theta}{\cos^2 \theta}$$

$$\Rightarrow \cos \theta \times \sin \theta = \sin \theta \times \cos \theta \quad \text{proved}$$

$$\textcircled{12i} (\sec A + \tan A)(1 - \sin A) = \cos A$$

$$\Rightarrow \sec A - \sec A \times \sin A + \tan A - \tan A \times \sin A$$

$$\Rightarrow \sec A - \frac{1}{\cos A} \times \sin A + \tan A - \frac{\sin A \times \sin A}{\cos A}$$

$$\Rightarrow \frac{1}{\cos A} - \frac{\sin A}{\cos A} + \frac{\sin A}{\cos A} - \frac{\sin^2 A}{\cos A}$$

$$\Rightarrow \frac{1 - \sin^2 A}{\cos A} \Rightarrow \frac{\cos^2 A}{\cos A}$$

$$\Rightarrow \cos A = \cos A \quad \text{proved!!}$$

$$\textcircled{ii} (1 + \tan^2 A)(1 - \sin A)(1 + \sin A) = 1$$

$$\Rightarrow \sec^2 A (1 + \sin A - \sin A - \sin^2 A) = 1$$

$$\Rightarrow \sec^2 A (1 - \sin^2 A) = 1$$

$$\Rightarrow \sec^2 A \times \cos^2 A = 1$$

$$\Rightarrow \frac{1}{\cos^2 A} \times \cos^2 A = 1$$

$$\Rightarrow \frac{1}{1} = 1 \text{ proved!!}$$

$$(13i) \tan A + \cot A = \sec A \operatorname{cosec} A$$

$$\Rightarrow \frac{\sin A}{\cos A} + \frac{\cos A}{\sin A} = \sec A \operatorname{cosec} A$$

$$\Rightarrow \frac{\sin^2 A + \cos^2 A}{\cos A \sin A} = \sec A \operatorname{cosec} A$$

$$\Rightarrow \frac{1}{\frac{1}{\sec A} \times \frac{1}{\operatorname{cosec} A}} = \sec A \operatorname{cosec} A$$

$$\Rightarrow \sec A \operatorname{cosec} A = \sec A \operatorname{cosec} A \text{ proved!!}$$

$$(ii) (1 - \cos A)(1 + \sec A) = \tan A \sin A$$

$$\Rightarrow 1 + \sec A - \cos A - \cos A \sec A = \tan A \sin A$$

$$\Rightarrow (1 - \cos A) \left[1 + \frac{1}{\cos A} \right] = \tan A \sin A$$

$$\Rightarrow (1 - \cos A) \left[\frac{\cos A + 1}{\cos A} \right] = \tan A \sin A$$

$$\Rightarrow \frac{\cancel{\cos A} + 1 - \cancel{\cos A} - \cos^2 A}{\cos A} = \tan A \sin A$$

$$\Rightarrow \frac{1 - \cos^2 A}{\cos A} = \tan A \sin A$$

$$\Rightarrow \frac{\sin^2 A}{\cos A} \Rightarrow \frac{\sin A \times \sin A}{\cos A} = \tan A \sin A$$

$$\Rightarrow \tan A \times \sin A = \tan A \sin A \text{ proved!}$$

$$(14i) \frac{1}{1 + \cos A} + \frac{1}{1 - \cos A} = 2 \operatorname{cosec}^2 A$$

$$\Rightarrow \frac{1 - \cancel{\cos A} + 1 + \cancel{\cos A}}{1^2 - \cos^2 A} = 2 \operatorname{cosec}^2 A$$

$$\Rightarrow \frac{2}{\sin^2 A} \Rightarrow \frac{2 \cdot 1}{\operatorname{cosec}^2 A} = 2 \operatorname{cosec}^2 A$$

$$\Rightarrow 2 \operatorname{cosec}^2 A = 2 \operatorname{cosec}^2 A \quad \text{proved!!}$$

$$\textcircled{\text{ii}} \quad \frac{1}{\sec A + \tan A} + \frac{1}{\sec A - \tan A} = 2 \sec A$$

$$\Rightarrow \frac{\sec A - \tan A + \sec A + \tan A}{\sec^2 A - \tan^2 A} = 2 \sec A$$

$$\Rightarrow \frac{2 \sec A}{1} = 2 \sec A \quad \text{proved!!}$$

$$\textcircled{15\text{i}} \quad \frac{\sin A}{1 + \cos A} = \frac{1 - \cos A}{\sin A}$$

$$\Rightarrow \frac{\sin A}{1 + \cos A} \times \frac{1 - \cos A}{1 - \cos A} = \frac{1 - \cos A}{\sin A}$$

$$\Rightarrow \frac{\sin A (1 - \cos A)}{1^2 - \cos^2 A} = \frac{1 - \cos A}{\sin A}$$

$$\Rightarrow \frac{\cancel{\sin A} (1 - \cos A)}{\cancel{\sin A}^2} = \frac{1 - \cos A}{\sin A}$$

$$\Rightarrow \frac{1 - \cos A}{\sin A} = \frac{1 - \cos A}{\sin A} \quad \text{proved!!}$$

$$\textcircled{\text{ii}} \quad \frac{1 - \tan^2 A}{\cot^2 A - 1} = \tan^2 A$$

$$\Rightarrow \frac{1 - 1}{\cot^2 A} = \tan^2 A$$

$$\Rightarrow \frac{\cot^2 A - 1}{\cot^2 A} = \tan^2 A$$

$$\Rightarrow \frac{\cancel{\cot^2 A} - 1}{\cot^2 A} \times \frac{1}{\cancel{\cot^2 A} - 1} = \tan^2 A$$

$$\Rightarrow \frac{1}{\cot^2 A} = \tan^2 A$$

$$\Rightarrow \tan^2 A = \tan^2 A \quad \text{proved!!}$$

$$\textcircled{\text{iii}} \quad \frac{\sin A}{1 + \cos A} = \operatorname{cosec} A - \cot A$$

$$\Rightarrow \frac{\sin A}{1 + \cos A} \times \frac{1 - \cos A}{1 - \cos A} = \operatorname{cosec} A - \cot A$$

$$\Rightarrow \frac{\sin A (1 - \cos A)}{1^2 - \cos^2 A} = \operatorname{cosec} A - \cot A$$

$$\Rightarrow \frac{\cancel{\sin A} (1 - \cos A)}{\sin^2 A} = \operatorname{cosec} A - \cot A$$

$$= \frac{1 - \cos A}{\sin A} = \operatorname{cosec} A - \cot A$$