

1Q) Consider two sets  $A = \{x \in \mathbb{Z} : |(|x-3| - 3)| \leq 1\}$

$$B = \left\{ x \in \mathbb{R} - \{1, 2\} : \frac{(x-2)(x-4)}{x-1} \log_e(|x-2|) = 0 \right\}$$

onto functions  $f: A \rightarrow B$

- i) 32                  ii) 79                  iii) 62                  iv) 81

2Q)  $\sum_{k=1}^n a_k = \alpha n^2 + \beta n$ . If  $a_{10} = 59$   
 $a_6 = 7a_1$ , then  $\alpha + \beta$  is  
evals to  ~~$\alpha + \beta$~~

- i) 12                  ii) 5                  iii) 7                  iv) 3

3Q)  $I(x) = \int \frac{3dx}{(4x+6)(\sqrt{4x^2+8x+3})}$  and  $I(0) = \frac{\sqrt{3}}{4} + 20$ . If

$$I\left(\frac{1}{2}\right) = \frac{a\sqrt{2}}{b} + c, \text{ where } a, b, c \in \mathbb{N}, \text{ gcd}(a, b) = 1$$

$a+b+c$  is eval to

- i) 28                  ii) 29                  iii) 31                  iv) 30

4) The sum of all the real solutions of the equation  $\log_{(x+3)}(6x^2+28x+30) = 5 - 2\log_{(6x+10)}(x^2+6x+9)$  is equal to.

- i) 2      ii) 4      iii) 1      iv) 0

5) The no. of ways, in which 16 oranges can be distributed to four children such that each child gets atleast one orange, is

- i) 455      ii) 429      iii) 384      iv) 403

6) If the points of intersection of the ellipses  $x^2+2y^2-6x-12y+23=0$  and  $4x^2+2y^2-20x-12y+35=0$  lie on a circle of radius  $r$  and centre  $(a,b)$  then the value of  $ab+18r^2$

- i) 51      ii) 52      iii) 55      iv) 53

7) Let  $\vec{a}, \vec{b}, \vec{c}$  be three vectors such that  $\vec{a} \times \vec{b} = 2(\vec{a} \times \vec{c})$ . If  $|\vec{a}|=1, |\vec{b}|=4, |\vec{c}|=2$ , and the angle b/w  $\vec{b}$  and  $\vec{c}$  is  $60^\circ$ , then  $|\vec{a} \cdot \vec{c}|$  is equal to

- i) 1      ii) 2      iii) 4      iv) 0

8) Let PQ be a chord of the hyperbola  $\frac{x^2}{4} - \frac{y^2}{b^2} = 1$ , perpendicular to the x-axis such that OPQ is an equilateral triangle, O being the centre of the hyperbola. If the eccentricity of the hyperbola is  $\sqrt{3}$ , then the area of the triangle OPQ is

- i)  $\frac{11}{5}$       ii)  $\frac{8\sqrt{3}}{5}$       iii)  $\frac{9}{5}$       iv)  $2\sqrt{3}$

9)  $\vec{a} = \hat{i} - 2\hat{j} + 3\hat{k}$ ,  $\vec{b} = 2\hat{i} + \hat{j} - \hat{k}$ ,  $\vec{c} = \lambda\hat{i} + \hat{j} + \hat{k}$  and  $\vec{v} = \vec{a} \times \vec{b}$ . If  $\vec{v} \cdot \vec{c} = 11$  and the length of the projection of  $\vec{b}$  on  $\vec{c}$  is P, then  $9P^2$  is equal to

- i) 9      ii) 6      iii) 12      iv) 4

10) If  $f(x) = \begin{cases} \frac{a|x| + x^2 - 2(\sin|x|)(\cos|x|)}{x}, & x \neq 0 \\ b, & x = 0 \end{cases}$  is continuous

at  $x=0$ , then  $a+b$  is equal to

- i) 0      ii) 1      iii) 4      iv) 2

11)  $z = \frac{\sqrt{3}}{2} + \frac{i}{2}$ ,  $i = \sqrt{-1}$ , then  $(z^{201} - i)^8$  is equal to

- i) 0      ii) 1      iii) 256      iv) -1

12)

12) Let  $A(1, 2)$  and  $C(-3, -6)$  be two diagonally opposite vertices of a rhombus, whose sides  $AD$  and  $BC$  are parallel to the line  $7x - y = 14$ . If  $B(\alpha, \beta)$  and  $D(\gamma, \delta)$  are the other two vertices, then  $|\alpha + \beta + \gamma + \delta|$  is equal to.

- i) 6      ii) 1      iii) 9      iv) 3

13) The area of the region enclosed between the circle  $x^2 + y^2 = 4$  and  $x^2 + (y-2)^2 = 4$  is:-

- i)  $\frac{4}{3}(2\pi - 3\sqrt{3})$       ii)  $\frac{2}{3}(2\pi - 3\sqrt{3})$       iii)  $\frac{4}{3}(2\pi - \sqrt{3})$       iv)  $\frac{2}{3}(4\pi - 3\sqrt{3})$

14) An equilateral triangle  $OAB$  is inscribed in the parabola  $y^2 = 4x$  with the vertex  $O$  at the vertex of the parabola. Then the minimum distance of the circle having  $AB$  as a diameter from the origin is.

- i)  $2(3 + \sqrt{3})$       ii)  $4(6 + \sqrt{3})$       iii)  $4(3 - \sqrt{3})$       iv)  $2(8 - 3\sqrt{3})$

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