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B.Tech. (CSE) VII Sem
CSPC-401- System Programming and Compiler Design

1. Indicate each of the following statements whether true or false, Justify your answer.
 - a) **True**, the semantic analyzer verifies the parse tree to ensure that it is meaningful and consistent with the rules of the programming language. It checks for semantic errors, such as type mismatches, undeclared variables, or incorrect function arguments, which cannot be detected during syntactic analysis.
 - b) **True**, every SLR(1) grammar is LR(0), but the reverse is not necessarily true. SLR(1) grammars consider follow sets to resolve conflicts, making them more powerful than LR(0) grammars, which do not. Therefore, an LR(0) grammar may not always be SLR(1).
 - c) **True**, Nondeterministic Finite Automata (NFA) and Deterministic Finite Automata (DFA) are equivalent in terms of the languages they can recognize. For every NFA, there exists a corresponding DFA that accepts the same language. This is established by the subset construction algorithm, which can convert an NFA to an equivalent DFA.
 - d) **True**, A DFA cannot count arbitrarily large numbers, including matching pairs of parentheses beyond a fixed limit. While it is possible to construct a DFA for a fixed number of pairs of parentheses (e.g., exactly three pairs).
 - e) **True**, this is because NFAs recognize regular languages, while context-free grammars can describe more complex languages, such as those with nested structures (e.g., balanced parentheses). Regular languages, which NFAs recognize, are a subset of context-free languages, but not all context-free languages are regular.

2. **True**, it groups the characters into meaningful tokens like keywords, identifiers, operators, or literals based on predefined rules. White spaces, operators, and special symbols act as boundaries that help the lexer separate tokens.
 - a) 19 different tokens
 - b) A grammar is typically defined as a 4-tuple: $G = (N, \Sigma, P, S)$
 - i. **N**: A finite set of **non-terminal symbols** (variables).
 - ii. **Σ** : A finite set of **terminal symbols**.
 - iii. **P**: A finite set of **production rules**.
 - iv. **S**: A **start symbol**
 - c)
 - i) The leftmost derivation for the string "**aaabbabbba**" is:
 $S \Rightarrow aB$
 $\Rightarrow aaBB$
 $\Rightarrow aaaBBB$
 $\Rightarrow aaabBB$
 $\Rightarrow aaabbB$
 $\Rightarrow aaabbaBB$

\Rightarrow aaabbabB
 \Rightarrow aaabbabbS
 \Rightarrow aaabbabbA
 \Rightarrow aaabbabbba

ii) The rightmost derivation for the string "aaabbabbba" is:

$S \Rightarrow aB$
 $\Rightarrow aaBB$
 $\Rightarrow aaBbS$
 $\Rightarrow aaBbbA$
 $\Rightarrow aaBbba$
 $\Rightarrow aaaBBbba$
 $\Rightarrow aaaBbSbba$
 $\Rightarrow aaaBbaBbba$
 $\Rightarrow aaaBbabbba$
 $\Rightarrow aaabbabbba$

3. Eliminate the left recursion from grammar(G1):

G1:
 $E \rightarrow EOT / T$
 $O \rightarrow + / -$
 $T \rightarrow TPF / F$
 $P \rightarrow *$
 $F \rightarrow (E) / id$

Step 1: Eliminate Left Recursion for E

$E \rightarrow TE'$
 $E' \rightarrow OTE' | \epsilon$

Step 2: Eliminate Left Recursion for T

$T \rightarrow FT'$
 $T' \rightarrow PFT' | \epsilon$

Final Transformed Grammar

After eliminating left recursion, we have the following grammar:

$E \rightarrow TE'$

$E' \rightarrow OTE' | \epsilon$

$O \rightarrow + \mid -$

$T \rightarrow FT'$

$T' \rightarrow PFT' \mid \epsilon$

$P \rightarrow *$

$F \rightarrow (E) \mid id$

Eliminate the left factoring from the grammar(G2):

G2:

$S \rightarrow f \mid fc \mid fcd \mid fcde$

Solution: After eliminating left factoring, the resulting grammar G2 is:

1. $S \rightarrow fS'$
2. $S' \rightarrow \epsilon \mid cS''$
3. $S'' \rightarrow \epsilon \mid dS'''$
4. $S''' \rightarrow \epsilon \mid e$

Ques(4): Rules for first set

1. If X is terminal, then $FIRST(X)$ is $\{X\}$.
2. If $X \Rightarrow \epsilon$ is a production, then add ϵ to $FIRST(X)$.
3. If X is nonterminal and $X \Rightarrow Y_1 Y_2 \dots Y_k$ is a production, then place a in $FIRST(X)$ if for some i , a is in $FIRST(Y_i)$, and ϵ is in all of $FIRST(Y_1), \dots, FIRST(Y_{i-1})$; that is, $Y_1, \dots, Y_{i-1} \Rightarrow \epsilon$. If ϵ is in $FIRST(Y_j)$ for all $j = 1, 2, \dots, k$, then add ϵ to $FIRST(X)$.

For example, everything in $FIRST(Y_1)$ is surely in $FIRST(X)$. If Y_1 does not derive ϵ , then we add nothing more to $FIRST(X)$, but if $Y_1 \Rightarrow \epsilon$, then we add $FIRST(Y_2)$ and so on.

Rules for follow set

1. Place $\$$ in $FOLLOW(S)$, where S is the start symbol and $\$$ is the input right end marker.
2. If there is a production $A \Rightarrow \alpha B\beta$, then everything in $FIRST(\beta)$, except for ϵ , is placed in $FOLLOW(B)$.
3. If there is a production $A \Rightarrow \alpha B$, or a production $A \Rightarrow \alpha B\beta$ where $FIRST(\beta)$ contains ϵ (i.e., $\beta \Rightarrow \epsilon$), then everything in $FOLLOW(A)$ is in $FOLLOW(B)$.

First and Follow for the Grammar G1.

G1:

$E \rightarrow EOT / T$

$O \rightarrow + / -$

$T \rightarrow TPF / F$

$P \rightarrow *$

$F \rightarrow (E) / id$

First Sets:

- $First(E) = \{(, id\}$
- $First(O) = \{+, -\}$
- $First(T) = \{(, id\}$
- $First(P) = \{*\}$
- $First(F) = \{(, id\}$

Follow Sets:

- $Follow(E) = \{+, -, \$,)\}$
- $Follow(O) = \{(, id\}$
- $Follow(T) = \{+, -, *,), \$\}$
- $Follow(P) = \{(, id\}$
- $Follow(F) = \{+, -, *,), \$\}$

Augmented Grammar G'

(3)

- $E' \rightarrow E$
- ① $E \rightarrow EOT$
- ② $E \rightarrow T$
- ③ $O \rightarrow +$
- ④ $O \rightarrow -$
- ⑤ $T \rightarrow TPF$
- ⑥ $T \rightarrow F$
- ⑦ $P \rightarrow *$
- ⑧ $F \rightarrow (E)$
- ⑨ $F \rightarrow id$

I_0

$$\begin{aligned} E' &\rightarrow \cdot E \\ E &\rightarrow \cdot EOT \\ E &\rightarrow \cdot T \\ T &\rightarrow \cdot TPF \\ T &\rightarrow \cdot F \\ F &\rightarrow \cdot (E) \\ F &\rightarrow \cdot id \end{aligned}$$

I_1 Goto(I_0, E)

$$\begin{aligned} E' &\rightarrow E \cdot \\ E &\rightarrow E \cdot OT \\ O &\rightarrow \cdot + \\ O &\rightarrow \cdot - \end{aligned}$$

I_2 Goto(I_0, T)

$$\begin{aligned} E &\rightarrow T \cdot \\ T &\rightarrow T \cdot PF \\ P &\rightarrow \cdot * \end{aligned}$$

I_3 Goto(I_0, F)

$$T \rightarrow F \cdot$$

I_4 Goto($I_0, ($)

$$\begin{aligned} F &\rightarrow (\cdot E) \\ E &\rightarrow \cdot EOT \\ E &\rightarrow \cdot T \\ T &\rightarrow \cdot TPF \\ T &\rightarrow \cdot F \\ F &\rightarrow \cdot (E), F \rightarrow \cdot id \end{aligned}$$

I_5 Goto(I_0, id)

$$F \rightarrow id \cdot$$

I_6 Goto(I_1, O)

$$\begin{aligned} E &\rightarrow EO \cdot T \\ T &\rightarrow \cdot TPF \\ T &\rightarrow \cdot F \\ F &\rightarrow \cdot (E) \\ F &\rightarrow \cdot id \end{aligned}$$

I_7 Goto($I_1, +$)

$$O \rightarrow + \cdot$$

I_8 Goto($I_1, -$)

$$O \rightarrow - \cdot$$

I_9 Goto(I_2, P)

$$\begin{aligned} T &\rightarrow TP \cdot F \\ F &\rightarrow \cdot (E) \\ F &\rightarrow \cdot id \end{aligned}$$

I_{10} Goto($I_2, *$)

$$P \rightarrow * \cdot$$

I_{11} Goto(I_4, E)

$$\begin{aligned} F &\rightarrow (E \cdot) \\ E &\rightarrow E \cdot OT \\ O &\rightarrow \cdot + \\ O &\rightarrow \cdot - \end{aligned}$$

I_{12} Goto(I_4, T)

$$\begin{aligned} E &\rightarrow T \cdot \\ T &\rightarrow T \cdot PF \\ P &\rightarrow \cdot * \end{aligned}$$

Goto(I_4, F)

I_{13} $\{ T \rightarrow F \cdot \}$

Goto($I_4, ($)

I_{14} $\left. \begin{aligned} F &\rightarrow (\cdot E) \\ E &\rightarrow \cdot EOT \\ E &\rightarrow \cdot T \\ T &\rightarrow \cdot TPF \\ T &\rightarrow \cdot F \\ F &\rightarrow \cdot (E) \\ F &\rightarrow \cdot id \end{aligned} \right\}$

I_{15} Goto(I_4, id)

$$F \rightarrow id \cdot$$

I_{12} Goto(I_6, T)

$$\begin{aligned} E &\rightarrow EOT \cdot \\ T &\rightarrow T \cdot PF \\ P &\rightarrow \cdot * \end{aligned}$$

I_{13} Goto(I_6, F)

$$T \rightarrow F \cdot$$

Goto($I_6, ($)

I_{14}

Goto(I_6, id)

I_{15}

I_{13} Goto(I_9, F)

$$T \rightarrow TPF \cdot$$

Goto($I_9, ($) = I_{14}

Goto(I_9, id) = I_{15}

Goto($I_{11}, ($)

I_{14} $F \rightarrow (E) \cdot$

Goto(I_{11}, O)

I_{16} $\left. \begin{aligned} E &\rightarrow EO \cdot T \\ T &\rightarrow \cdot TPF \\ T &\rightarrow \cdot F \\ F &\rightarrow \cdot (E) \\ F &\rightarrow \cdot id \end{aligned} \right\}$

Goto($I_{11}, +$) = I_{17}

Goto($I_{11}, -$) = I_{18}

Goto(I_{12}, P)

I_{19} $\left. \begin{aligned} T &\rightarrow TP \cdot F \\ F &\rightarrow \cdot (E) \\ F &\rightarrow \cdot id \end{aligned} \right\}$

Goto($I_{12}, *$) = I_{20}

Total Item Sets
from I_0 to I_{14}
 $\hookrightarrow I_{15}$

| | + | - | * | id | (|) | \$ | E | O | T | P | F |
|----------|-------|-------|-----------|-------|-------|-------|---------------|-------|----|---|---|----|
| I_0 | | | | S_9 | S_8 | | | 1 | | 2 | | 3 |
| I_1 | S_3 | S_4 | | | | | <u>Accept</u> | 6 | | | | |
| I_2 | r_2 | r_2 | $S_7 r_2$ | r_2 | r_2 | r_2 | r_2 | | | 9 | | |
| I_3 | r_6 | r_6 | r_6 | | | | r_6 | r_6 | | | | |
| I_4 | | | | S_9 | S_8 | | | 11 | | 2 | | 3 |
| I_5 | r_9 | r_9 | r_9 | | | | r_9 | r_9 | | | | |
| I_6 | | | | S_9 | S_8 | | | | 12 | | | 3 |
| I_7 | | | | r_3 | r_3 | | | | | | | |
| I_8 | | | | r_4 | r_4 | | | | | | | |
| I_9 | | | | S_9 | S_8 | | | | | | | 13 |
| I_{10} | | | S_7 | r_7 | r_7 | | | | | | | |
| I_{11} | S_3 | S_4 | | | | | S_8 | 6 | | | | |
| I_{12} | r_1 | r_1 | $S_7 r_1$ | | | | r_1 | r_1 | | 9 | | |
| I_{13} | r_5 | r_5 | r_5 | | | | r_5 | r_5 | | | | |
| I_{14} | | | | r_8 | r_8 | | | | | | | |

Given Grammar is not LR(0) \because There are two S/R conflict
 But G_1 is SLR(1)

G(a): $E \rightarrow T + E / T$

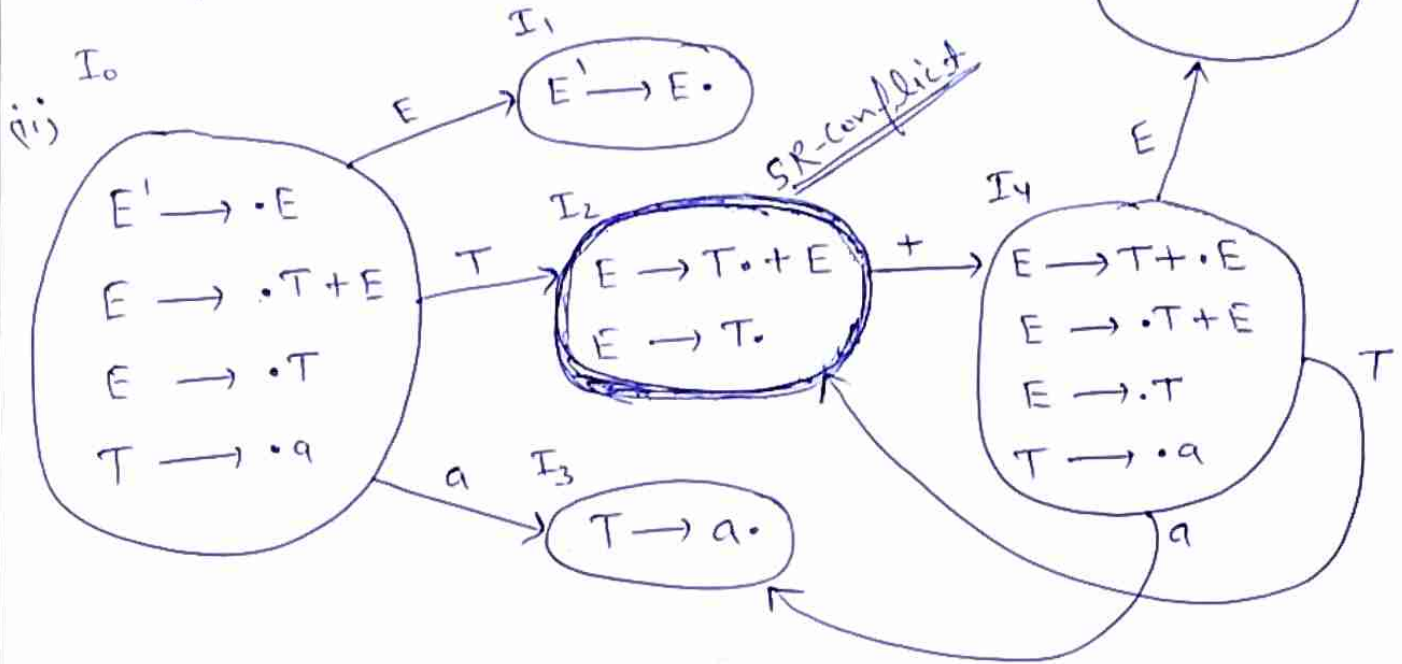
$T \rightarrow a$

(i) $E' \rightarrow E$

$E \rightarrow T + E$

$E \rightarrow T$

$T \rightarrow a$



I_2 : Contain SR conflict so it is not LR(0) grammar.

G(b): $E \rightarrow E + T / T$

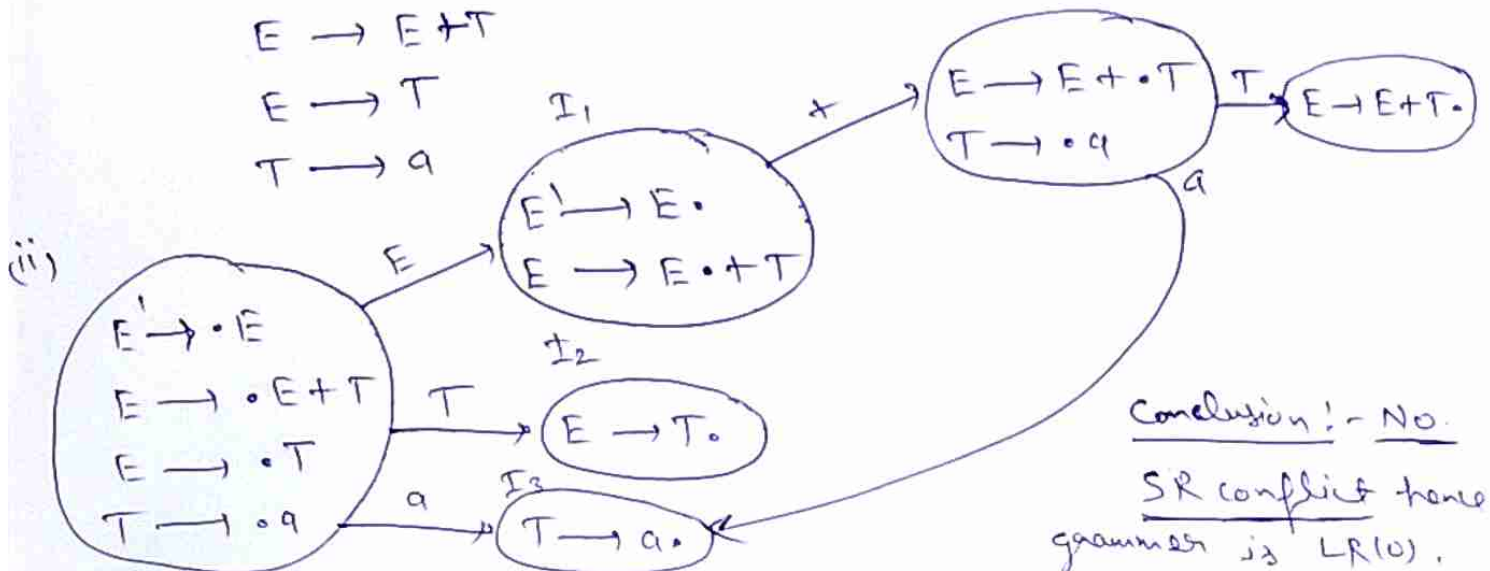
$T \rightarrow a$

(i) $E' \rightarrow E$

$E \rightarrow E + T$

$E \rightarrow T$

$T \rightarrow a$



Conclusion: - No SR conflict hence grammar is LR(0).